

A Computationally Efficient Multi-coset Wideband Radar ESM Receiver

Mehrdad Yaghoobi and Mike E. Davies

Edinburgh Research Partnership in Signal and Image Processing

Institute for Digital Communications,

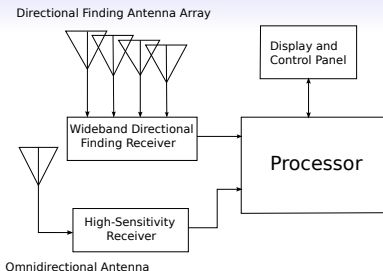
The University of Edinburgh

NATO SET-213 Specialist Meeting, 12 May, 2014



Engineering and Physical Sciences
Research Council

Electronic Support Measures (ESM)



- **Task:** detecting all RF emitters to identify the presence of threats.
- It has a **passive** monitoring system.
- While ESM signals are **very dense**, e.g. can be hundreds of thousands of pulses per second, they have **very sparse** TF representations.
- ESM systems can be noise limited, rather than sparsity limited.

Conventional Techniques for ESM Receivers



- **Instantaneous Frequency Measurements:** limited spectral sensitivity.
- **Rapid Frequency Sweeping ADC's:** limited temporal sensitivity.
- **Wideband Analog to Digital Converters:** need multi GHz ADC's.
- **Proposal:** Sub-Nyquist Analog to Information Converter.

Sub-Nyquist Sampling

- Why?

- ① Sampling at the rate of Nyquist is **difficult** or **costly** in some applications, *e.g.* Wideband ADC's and Wideband Digital Receivers.
- ② It is a **waste of resources**, if we sample at a rate, much higher than the information rate.
- ③ An **application specific** sampling strategy, *i.e.* exploring signal structures.

- How?

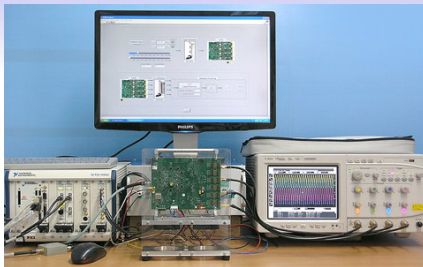
- ① Using underlying signal structures, *e.g.* sparsity.
- ② Incorporating non-uniform sampling (random?) in the sensing framework.
- ③ Non-linear reconstruction of signals.

Sub-Nyquist Sampling, cont

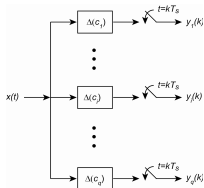
- **Challenges?**

- ① *Analog Hardware*: How efficiently can we design the analog part?
- ② *Computational Complexity*: How efficient can we implement the non-linear recovery algorithm?
- ③ *Noise Sensitivity*: Sensitivity to the input noise?
- ④ *Robustness*: How much the sub-Nyquist algorithm is sensitive to the **signal model mismatch** and **circuit design tolerances**.

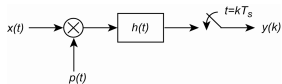
Sub-Nyquist Sampling Techniques



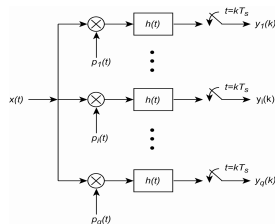
Technion Modulated Wideband Converter Demonstrator



Multi-coset Sampling
(Feng&Bresler 1996)



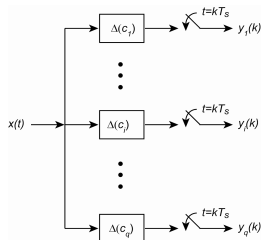
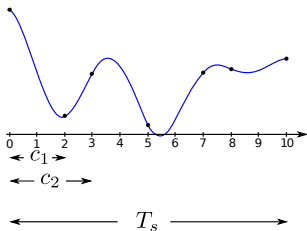
Random Demodulator
(Triopp et al. 2007)



Modulated Wideband Converter
(Mishali and Eldar 2010)

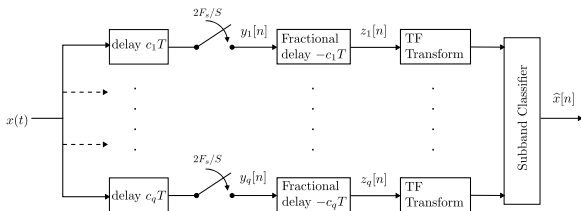
Multi-coset Sampling Framework

- **Non-uniform** sampling technique [Feng and Bresler, 1996].
- Sparse multiband signal model.
- A **subspace method** for reconstruction by Feng et al.
- A **convex optimisation** problem for reconstruction by [Mishali and Eldar 2009].



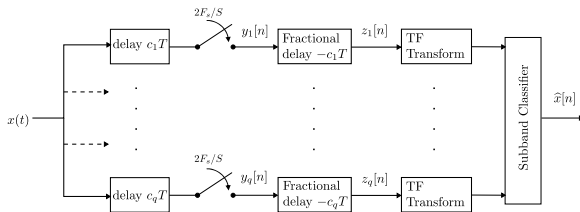
Proposed Sub-Nyquist Sampling Framework

- A Multi-coset sampling strategy.
- Avoiding any complicated operations e.g. SVD, ℓ_1 minimisation.
- The signal model has to fit into the ESM.

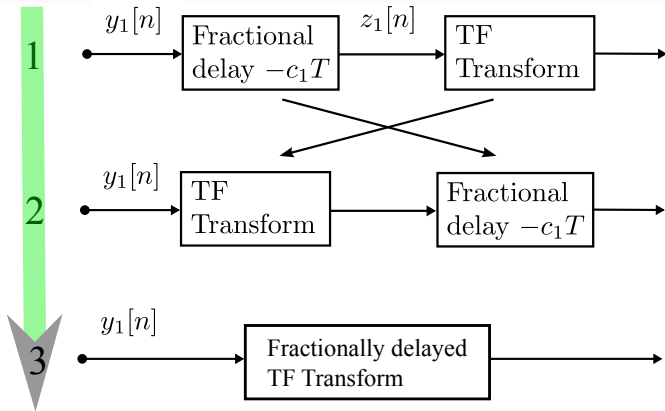


Components of Proposed Framework

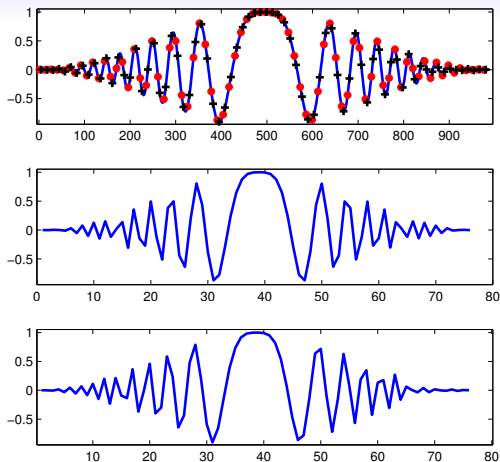
- *A bank of multi-coset channels:* it has distinguished delays.
- *Digital Fractional Delay (DFD) filters.*
- *Time-Frequency transform:* STFT has currently been used.
- *Subband Classifier:* Composed of a linear operator (Harmonic Frame), followed by a simple maximum-absolute value operator.



Digital Fractional Delay Implementation

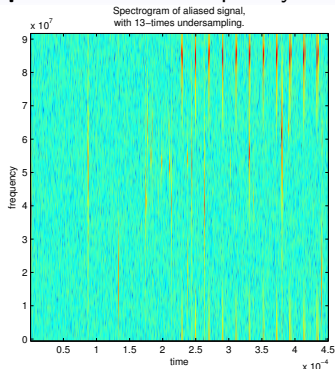
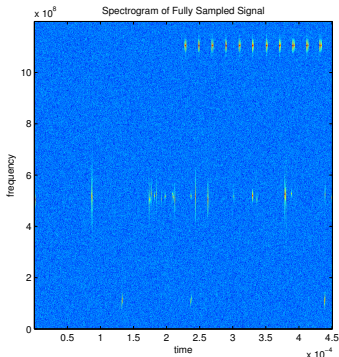


Discretisation of Time-Frequency Kernel



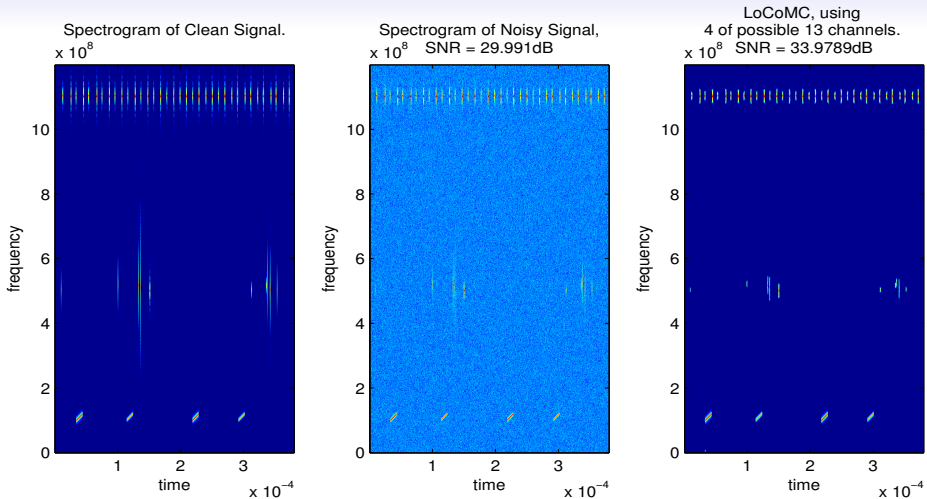
Assumptions and Properties

- **Approximate Disjoint Aliased Support:** different to sparsity.



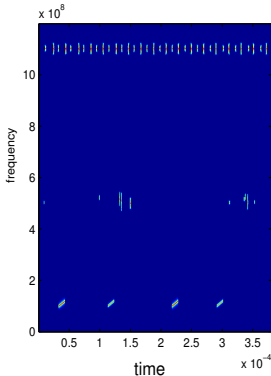
- **No random sampling:** optimal delay parameters from a Harmonic Equiangular Tight Frame (HETF).
- **No DFD filter:** absorption into TF transform.

Evaluation with Radar ESM signals

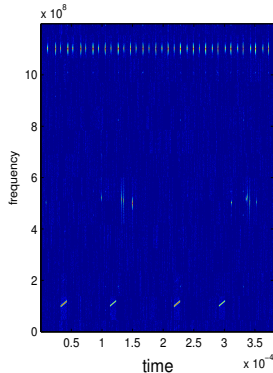


Comparison with Other Methods

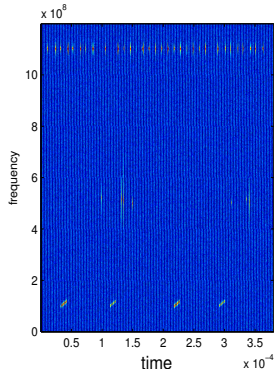
LoCoMC, 4 Channels.
Undersampling Factor of 13. SNR = 34.1052



Spectrogram of reconstructed signal by windowed MUSIC,
using 4 channels. SNR = 26.8553

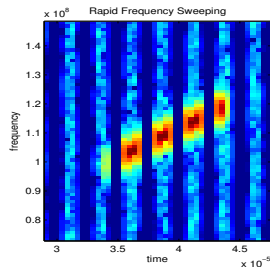
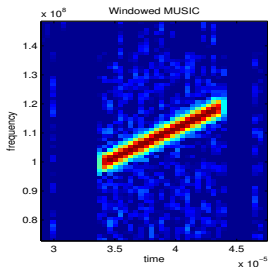
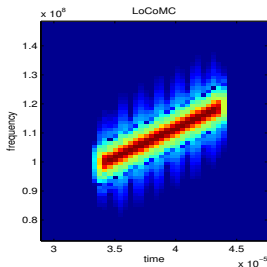
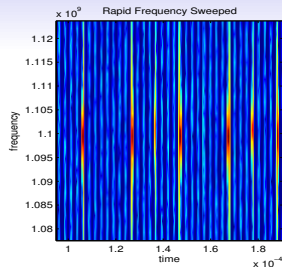
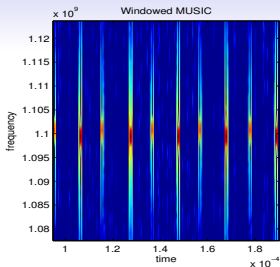
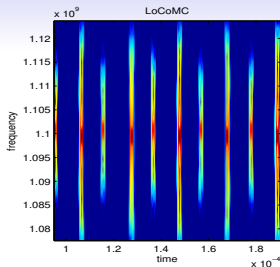


Rapid Frequency Sweeping, 2 Channel(s),
Undersampling Factor of 6. SNR = 3.2083



- Two overlapping ADC's with 1/6 of Nyquist sampling rate for RFS method.

Comparison with Rapid Frequency Sweeping



LoCoMC at a Glance:

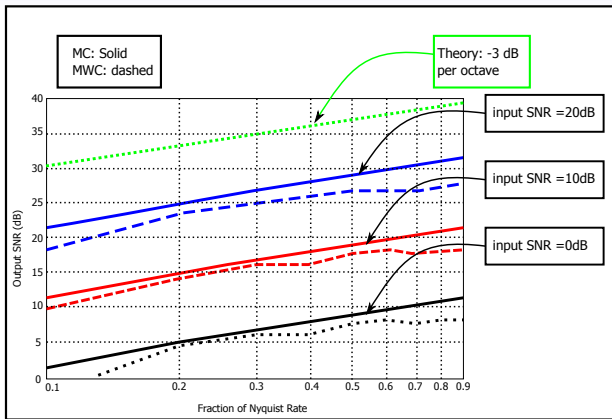
- **Pros:**

- **Non-iterative:** it may be pipelined.
- Can use only **a few** Multi-coset channels, e.g. as few as $q = 2$.
- Uses a different signal model, *i.e.* **ADAS**, which matches well to some classes of signals, e.g. ESM.
- **Large Dynamic Range**, e.g. 70 dB, which makes it suitable for the low probability of intercept signals.
- **Continuously monitoring** wideband RF signals, in a contrast with the rapid frequency sweeping technique.

- **Cons:**

- **Noise folding:** 3 dB processing gain loss per octave. A characteristic of sub-Nyquist sampling techniques.
- Needs a **Fast** “sampler”. The “holder/tracker” can be slow.

Noise Folding in Sub-Nyquist Sampling



Conclusion and Future Work

- **Conclusion:**

- A low SWAP algorithm for radar ESM receiver.
- Exploring parsimonious structure of ESM signals.
- When ESM signals are ADAS, the signal recovery is guaranteed.
- Outperforms the MUSIC recovery algorithm in the given ESM signals.

- **Future work:**

- An optimal TF transform to maximise coherent processing gain.
- Sensitivity and robustness analysis.
- Pulse descriptor word extraction.
- Designing Hardware Demonstrator.



Thanks for your attention.